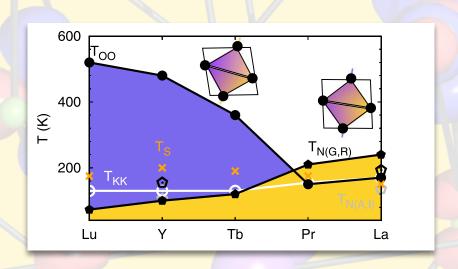
Kugel-Khomskii materials: flipping the order of transitions



Eva Pavarini

Forschungszentrum Jülich Peter Grünberg Institute

spontaneous ordering of orbitals

Crystal structure and magnetic properties of substances with orbital degeneracy

K. I. Kugel' and D. I. Khomskii P. N. Lebedev Physics Institute (Submitted November 13, 1972) Zh. Eksp. Teor. Fiz. 64, 1429-1439 (April 1973)



Exchange interaction in magnetic substances containing ions with orbital degeneracy is considered. It is shown that, among with spin ordering, superexchange also results in cooperative ordering of Jahn-Teller ion orbitals, which, generally speaking, occurs at a higher temperature and is accompanied by distortion of the lattice (which is a secondary effect here). Concrete studies are performed for substances with a perovskite structure (KCuF₃, LaMnO₃, MnF₃). The effective spin Hamiltonian is obtained for these substances and the properties of the ground state are investigated. The orbital and magnetic structures obtained in this way without taking into account interaction with the lattice are in accord with the structures observed experimentally. The approach employed also permits one to explain the strong anisotropy of the magnetic properties of these compounds and to obtain a reasonable estimate for the critical temperatures.

KCuF₃

LaMnO₃

strong Coulomb repulsion (the Hubbard U)

+ orbitals degrees of freedom

= orbital super-exchange



orbital ordering and orbital physics

CORRELATED ELECTRON SYSTEMS

Orbital Physics in Transition-Metal Oxides

Y. Tokura^{1,2} and N. Nagaosa¹

An electron in a solid, that is, bound to or nearly localized on the atomic site, has three attributes: charge, spin, and orbital. Th represents the shape of the electron cloud in solid. In transition oxides with anisotropic-shaped d-orbital electrons, the Coulomb tion between the electrons (strong electron correlation effection importance for understanding their metal-insulator transitions a erties such as high-temperature superconductivity and colossal toresistance. The orbital degree of freedom occasionally plays a tant role in these phenomena, and its correlation and/or order transition causes a variety of phenomena through strong coup charge, spin, and lattice dynamics. An overview is given here "orbital physics," which will be a key concept for the science a nology of correlated electrons.

103, 067205 (2009)

PHYSICAL RE

Magnetically Hidden Order of Kra

George Jackeli* and Giniyat Khaliullin

Max-Planck-Institut für Festkörperforschung, Heisenbergstrasse 1, D-70569 Stuttgart, Germany (Received 10 June 2009; published 7 August 2009)

We formulate and study an effective Hamiltonian for low-energy Kramers doublets of d^1 ions on a square lattice. We find that the system exhibits a magnetically hidden order in which the expectation values of the local spin and orbital moments both vanish. The order parameter responsible for a timereversal symmetry breaking has a composite nature and is a spin-orbital analog of a magnetic octupole. We argue that such a hidden order is realized in the layered perovskite Sr₂VO₄.

DOI: 10.1103/PhysRevLett.103.067205

PACS numbers: 75.30.Et. 71.70.Ei. 75.10.Jm

TRANSITION METAL OXIDES

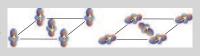
Ferroelectricity driven by orbital order

The discovery that the rotation of the orbital arrangement in manganites induces ferroelectricity exposes an intriguing phase transition that could serve as a blueprint for novel applications.

BERNHARD KEIMER

Heisenbergstr. 1, 70569 Stuttgart, Germany

sition metal oxides have fascinated scientists since the 1950s, when the newly developed technique of neutron diffraction was used to show that the compound La_{1, L}(a,MnU₂ exhibits a rich variety of structural and magnetic phases as the Ca concentration is tuned. The fascination has increased in the wake of the discovery of high-temperature superconductivity in a chemically similar compound,



show that the compound La. Ca.MnO, exhibits a rich Figure 1 Possible arrangements of Mn²⁺ d-orbitals on a square lattice. The patterns

PHYSICAL REVIEW LETTERS

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30 OCTOBER 2000

[PDF] 1 Metal-Insulator Transition and Orbital Order in ... - arXiv...

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Orbital Liquid in Three-Dimensional Mott Insulator: LaTiO₃

G. Khaliullin^{1,2} and S. Maekawa²

¹Max-Planck-Institut für Festkörperforschung, Heisenbergstrasse 1, D-70569 Stuttgart, Germany ²Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan (Received 5 June 2000)

of spin and orbital states in Mott insulator LaTiO3. The spin-orbital superexchange (t_{2g}) ions in cubic crystal suffers from a pathological degeneracy of orbital states Quantum effects remove this degeneracy and result in the formation of the coherent the orbital moment of t_{2g} level is fully quenched. We find a finite gap for orbital sordered state of local degrees of freedom on unfrustrated, simple cubic lattice is al liquid state naturally explains observed anomalies of LaTiO₃.

es of spin and

VOLUME 85, NUMBER 18

PRL 99, 156401 (2007)

Satoshi Okamoto & Andrew J. Millis

Department of Physics, Columbia University 538 New York 10027, USA

insulator and a band in

Electronic reconstruction at

an interface between a Mott

Surface science is an important and we materials science involving the study

Superexchange Interaction in Orbitally Fluctuating RVO₃

PHYSICAL REVIEW LETTERS

J.-S. Zhou and J. B. Goodenough

Texas Materials Institute, University of Texas at Austin, Austin, Texas 78712, USA

J.-O. Yan

Ames Laboratory, Ames, Iowa 50011, USA

Y. Ren

Advanced Photon Source, Argonne National Laboratory, Argonne, Illinois 60439, USA (Received 18 May 2007; published 8 October 2007)

OCTOBER 2007 etal oxides

ülich, Germany). **Orbital** les, and vet its.

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ngular lattice system ueen et al. [Phys.

tion-metal ... fornia. Los Angeles 🔻

resonant X-ray scattering techniques in which the 3d orbital order is detected by its ffect on excited (in states [8]. The case for orbital ordering has been

ECS Journal of Solid State Science and Technology, 2022 11 054004 2162-8777/2022/11(5)/054004/16/\$40.00 © 2022 The Electrochemical Society ("ECS"), Published on behalf of ECS by IOP Publishing Limited





Review—Orbital Physics: Glorious Past, Bright Future

D. I. Khomskii^z

II. Physikalisches Institut, Universität zu Köln, 50937 Köln, Germany

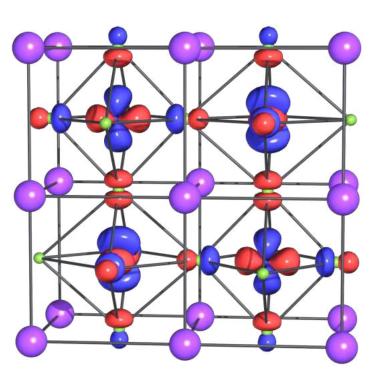
Transition metal (TM) compounds present a very big class of materials with quite diverse properties. There and systems with insulator-metal transitions among them; most magnetic systems are TM compounds; t superconductors among them. Their very rich properties are largely determined by the strong interplay freedom: charge; spin; orbital; lattice. Orbital effects play a very important role in these systems—and not of of this field, initiated by Goodenough almost 70 years ago, turned out to be very fruitful and produced a lot this short review I discuss the basics of orbital physics and summarize the main achievements in the Goodenough played a pivotal role, and which are nowadays widely used to explain many properties of TM of part of the text I discuss novel developments and perspectives in orbital physics, which is still a very a constantly producing new surprises.

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the secondary effect

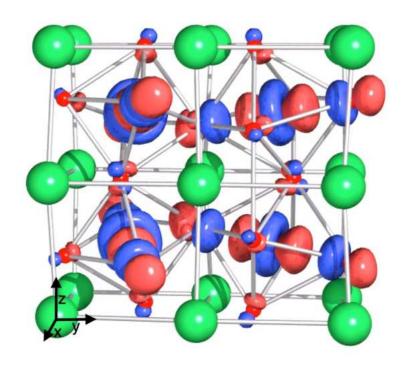
co-operative Jahn-Teller-like distortion

KCuF₃



 $t_{2g}^6 e_g^3$ G-type OO

LaMnO₃



 $t_{2g}^3e_g^1$

C-type OO



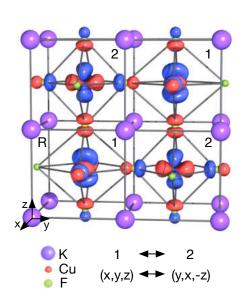
but there is the Jahn-Teller theorem

Crystal Distortion in Magnetic Compounds

JUNJIRO KANAMORI*

Institute for the Study of Metals, University of Chicago, Chicago 37, Illinois

The crystal distortion which arises from the Jahn-Teller effect is discussed in several examples. In the case of compounds containing Cu²+ or Mn³+ at octahedral sites, the lowest orbital level of these ions is doubly degenerate in the undistorted structure, and there is no spin-orbit coupling in this level. It is shown that, introducing a fictitious spin to specify the degenerate orbital states, we can discuss the problem by analogy with the magnetic problems. The "ferromagnetic" and "antiferromagnetic" distortions are discussed in detail. The transition from the distorted to the undistorted structure is of the first kind for the former and of the second kind for the latter. Higher approximations are discussed briefly. In compounds like FeO, CoO, and CuCr₂O₄, the lowest orbital level is triply degenerate, and the spin-orbit coupling is present in this level. In this case the distortion is dependent on the magnitude of the spin-orbit coupling relative to the strength of the Jahn-Teller effect term. The distortion at absolute zero temperature and its temperature dependence are discussed.



$$|\theta\rangle = \sin\frac{\theta}{2}|3z^2 - 1\rangle + \cos\frac{\theta}{2}|x^2 - y^2\rangle$$



a small CF splitting can be enough!

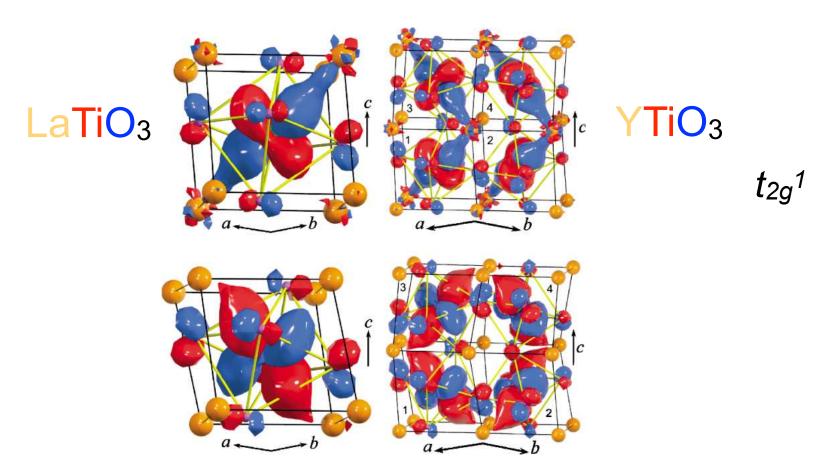
VOLUME 92, NUMBER 17

PHYSICAL REVIEW LETTERS

week ending 30 APRIL 2004

Mott Transition and Suppression of Orbital Fluctuations in Orthorhombic $3d^1$ Perovskites

E. Pavarini, S. Biermann, A. Poteryaev, A. I. Lichtenstein, A. Georges, and O. K. Andersen

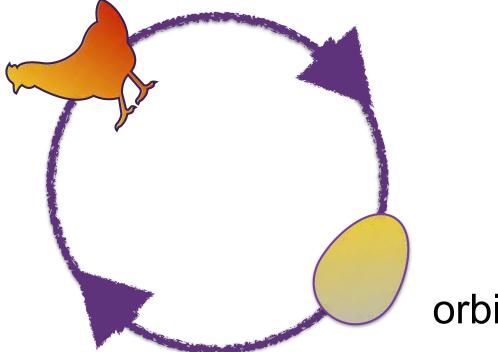




Kugel-Khomskii materials?

a chicken-and-egg problem

distortions



orbital ordering



(i) are there true Kugel-Khomskii materials?

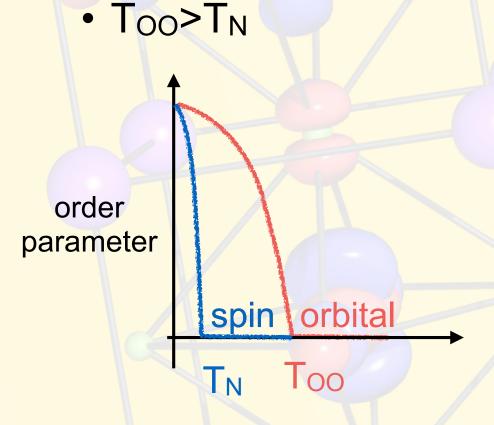
and how do we identify them?

a chicken-and-egg problem

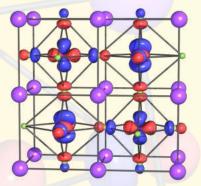


(ii) why Too>Tn?

can one flip the transitions?



KCuF₃



TN~40 K TOO~1400 K

cDMFT/QMC on JURECA

$$H = -\sum_{ii'} \sum_{mm'} \sum_{\sigma} t^{ii'}_{mm'} c^{\dagger}_{im\sigma} c_{i'm'\sigma}$$

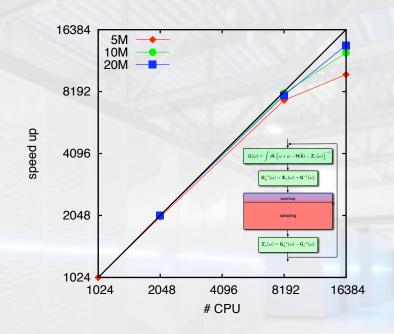
$$+ U \sum_{im} n_{im\uparrow} n_{im\downarrow}$$

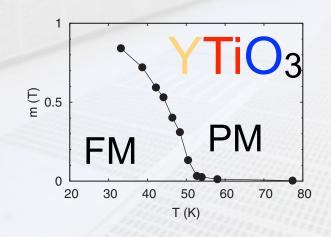
$$+ \frac{1}{2} \sum_{im\neq m'\sigma\sigma'} (U - 2J - J\delta_{\sigma\sigma'}) n_{im\sigma} n_{im'\sigma'}$$

$$- J \sum_{m\neq m'} (c^{\dagger}_{m\uparrow} c^{\dagger}_{m'\downarrow} c_{m'\uparrow} c_{m\downarrow} + c^{\dagger}_{m\uparrow} c^{\dagger}_{m\downarrow} c_{m'\uparrow} c_{m'\downarrow})$$

DMFT and cDMFT generalized QMC solvers:

- ◆ CT-HYB: A. Flesch, E. Gorelov, E. Koch and E. Pavarini Phys. Rev. B 87, 195141 (2013)
- ◆ CT-INT: E. Gorelov et al, PRL 104, 226410 (2010)
- ◆ CT-INT+SO: G. Zhang, E. Gorelov, E. Sarvestani, and E. Pavarini, Phys. Rev. Lett. 116, 106402 (2016)





solution of chicken and egg problem

PRL 101, 266405 (2008)

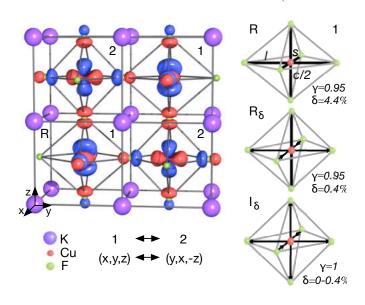
PHYSICAL REVIEW LETTERS

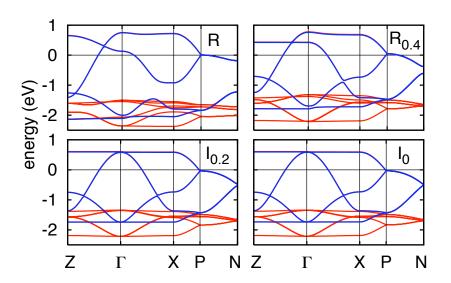
week ending 31 DECEMBER 2008

Mechanism for Orbital Ordering in KCuF₃

E. Pavarini, ¹ E. Koch, ¹ and A. I. Lichtenstein ²

¹Institut für Festkörperforschung and Institute for Advanced Simulation, Forschungzentrum Jülich, 52425 Jülich, Germany ²Institute of Theoretical Physics, University of Hamburg, Jungiusstrasse 9, 20355 Hamburg, Germany (Received 18 August 2008; published 31 December 2008)



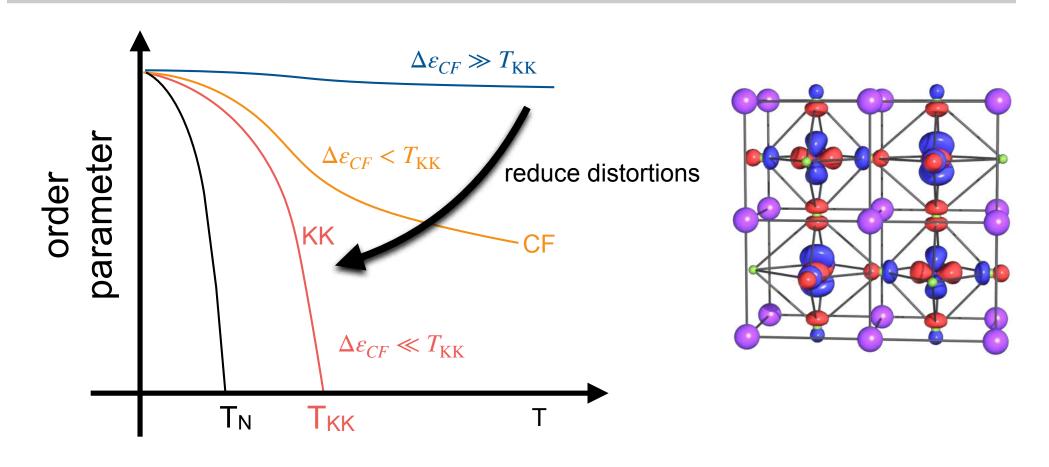


to single out KK effects:

- (i) progressively reduce distortion (hence CF splitting)
- (ii) calculate order parameter vs temperature



order parameter vs temperature



if KK is the mechanism: $T_{OO} \sim T_{KK}$



 $KCuF_3$ $T_N \sim 40 K$ $T_{00} \sim 1400 K$



KK SE large but not sufficient alone

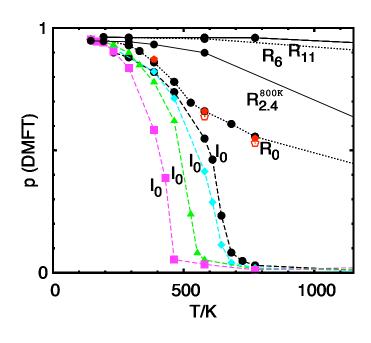
KCuF₃

Order Darameter (DMF) of 1000 1500 T/K

Phys. Rev. Lett. 101, 266405 (2008)

 $T_{KK} \sim 350 \text{ K} \ll T_{OO} \sim 1400 \text{ K}$

LaMnO₃



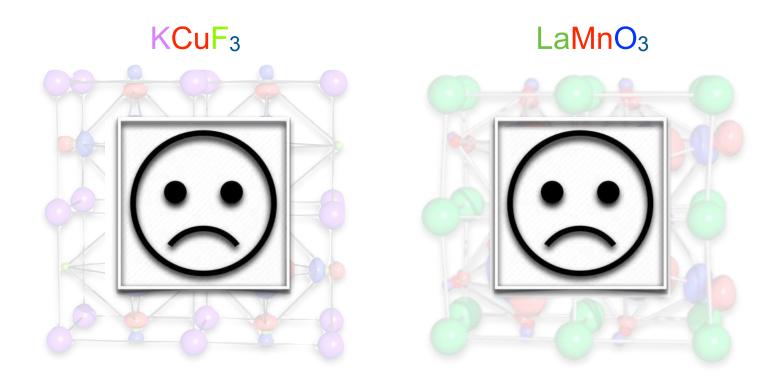
Phys. Rev. Lett. **104**, 086402 (2010)

 $T_{KK} \sim 600 \ K \ll T_{OO} \sim 1200 \ K$



so far for eg systems...

KK super-exchange large but not sufficient to explain ordering at high temperature

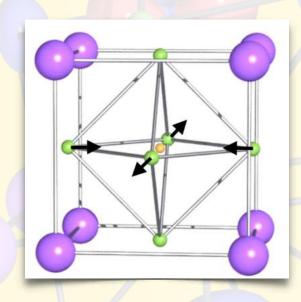


(and many more systems)

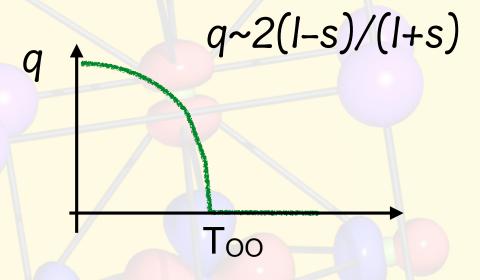


KCuF₃ not a true KK material

... but also not a true Jahn-Teller system!



I= long CuF bond s= short CuF bond

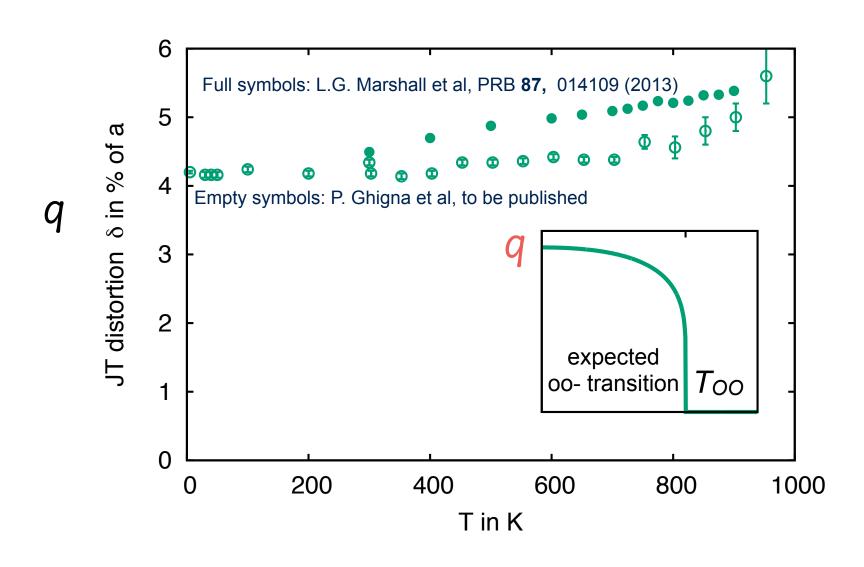




experiments: q increases with temperature

theory reproduce this behavior

PRB **96**, 054107 (2017)

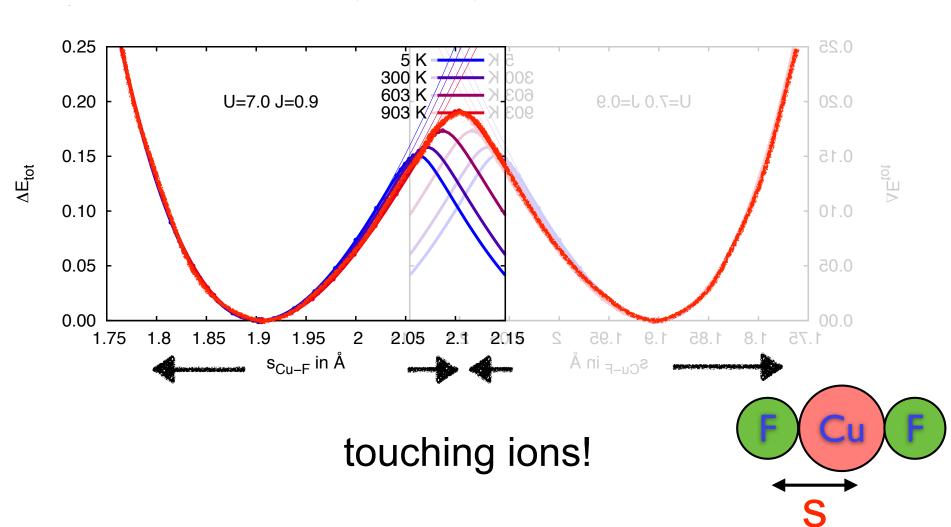


the *T*-dependence is via the lattice constant!

PHYSICAL REVIEW B **96**, 054107 (2017)

Thermally assisted ordering in Mott insulators

Hunter Sims,¹ Eva Pavarini,^{2,3} and Erik Koch^{1,2,3,*}



(i) are there true Kugel-Khomskii materials?

and how do we identify them?

a chicken-and-egg problem



let us change perspective

focus on electronic effects only

candidates: t2g systems

larger orbital degeneracy, smaller electron-lattice coupling, smaller crystal-field coupling

augment DMFT with general SE Hamiltonians

PHYSICAL REVIEW B 102, 035113 (2020)

Origin of orbital ordering in YTiO₃ and LaTiO₃

Xue-Jing Zhang, Erik Koch, and Eva Pavarini Institute for Advanced Simulation, Forschungszentrum Jülich, 52425 Jülich, Germany

(Received 14 April 2020; accepted 15 June 2020; published 6 July 2020)

The origin of orbital order in correlated transition-metal compounds is strongly debated. For the paradigmatic e_g systems KCuF₃ and LaMnO₃, it has been shown that the electronic Kugel'-Khomskii mechanism alone is not sufficient to drive the orbital-ordering transition up to the high temperatures at which it is experimentally observed. In the case of t_{2g} compounds, however, the role played by the superexchange interaction remains unclear. Here we investigate this question for two representative systems, the 3d t_{2g}^1 Mott insulators LaTiO₃ and YTiO₃. We show that the Kugel'-Khomskii superexchange transition temperature T_{KK} is unexpectedly large, comparable to the value for the e_g^3 fluoride KCuF₃. By deriving the general form of the orbital superexchange

PHYSICAL REVIEW B 105, 115104 (2022)

General superexchange Hamiltonians for magnetic and orbital physics in e_g and t_{2g} systems

Xue-Jing Zhang, ¹ Erik Koch, ^{1,2} and Eva Pavarini ^{1,2,*}

¹Institute for Advanced Simulation, Forschungszentrum Jülich, 52425 Jülich, Germany

²JARA High-Performance Computing, 52062 Aachen, Germany.

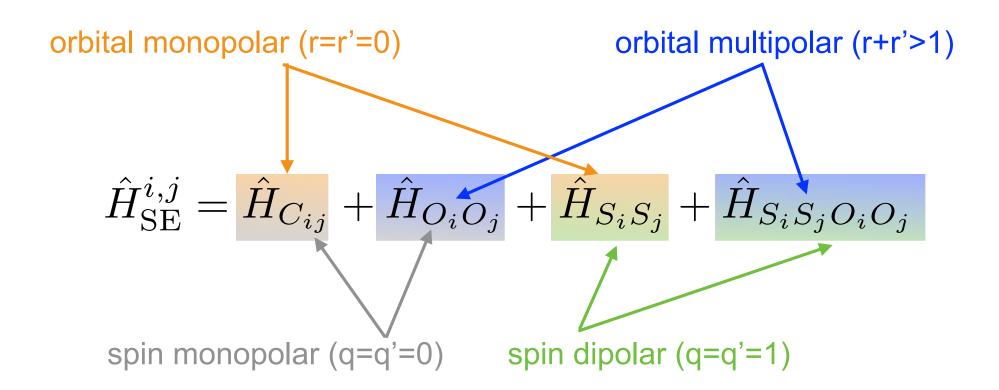
(Received 6 December 2021; accepted 16 February 2022; published 3 March 2022)

Material-specific super-exchange Hamiltonians are the key to studying spin and orbital physics in strongly correlated materials. Recently, via an irreducible-tensor operator representation, we derived the orbital superexchange Hamiltonian for t_{2g}^1 perovskites and successfully used it, in combination with many-body approaches, to explain orbital physics in these systems. Here, we generalize our method to e_g^n and t_{2g}^n systems at arbitrary integer filling n, including both spin and orbital interactions. The approach is suitable for numerical implementations



multipolar super-exchange expansion

$$\hat{H}_{\mathrm{SE}}^{i,j} = \sum_{qq'} \sum_{\nu\nu'} \sum_{rr'} \sum_{\mu\mu'} \hat{\tau}_i^{r\mu;q\nu} D_{r\mu,r'\mu'}^{ij;q\nu} \hat{\tau}_j^{r'\mu';q\nu}$$
 r: orbital rank q:spin rank

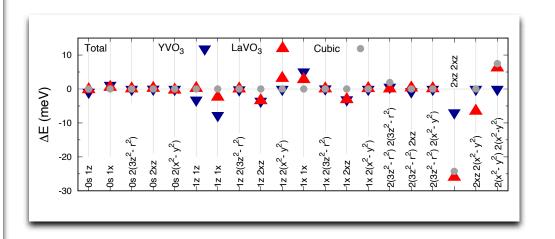




irreducible tensor decomposition

$$\hat{H}_{SE}^{i,j} = \sum_{qq'} \sum_{\nu\nu'} \sum_{rr'} \sum_{\mu\mu'} \hat{\tau}_i^{r\mu;q\nu} D_{r\mu,r'\mu'}^{ij;q\nu} \hat{\tau}_j^{r'\mu';q\nu}$$

r μ	$r' \mu'$	t_{2g}^1	t_{2g}^2	$D^{ij}_{r\mu,r'\mu'} imes U/2$	
0 s	0 s	$-\mathcal{W}_0$	$-\mathcal{V}_0$		$(t_{xz,xz}^2 + t_{yz,yz}^2 + t_{xy,xy}^2)$
0 s	1 z	$-\mathcal{W}_1$	$-\mathcal{V}_1$	$\frac{\sqrt{2}}{\sqrt{3}}$	$\left(t_{xz,xz}^2 - t_{yz,yz}^2\right)$
0 s	$2 z^2$	$-\mathcal{W}_1$	$-\mathcal{V}_1$	$\frac{\sqrt{2}}{3}$	$(t_{xz,xz}^2 + t_{yz,yz}^2 - 2t_{xy,xy}^2$
1 z	1 z	$+\mathcal{W}_2$	$+\mathcal{V}_2$		$\left(t_{xz,xz}^{2}+t_{yz,yz}^{2}\right)$
1 z	$2 z^2$	$+\mathcal{W}_2$	$+\mathcal{V}_2$	$\frac{1}{\sqrt{3}}$	$\left(t_{xz,xz}^2 - t_{yz,yz}^2\right)$
$2 z^2$	$2 z^2$	$+\mathcal{W}_2$	$+\mathcal{V}_2$	1/3	$(t_{xz,xz}^2 + t_{yz,yz}^2 + 4t_{xy,xy}^2$
1 x	1 x	$+\mathcal{W}_2$	$+\mathcal{V}_2$	-	$(t_{xz,xz}+t_{yz,yz})t_{xy,xy}$
2 xz	2 xz	$+\mathcal{W}_2$	$+\mathcal{V}_2$		$(t_{xz,xz}+t_{yz,yz})t_{xy,xy}$
1 x	2 xz	$+\mathcal{W}_2$	$+\mathcal{V}_2$		$(t_{xz,xz}-t_{yz,yz})t_{xy,xy}$
$2 x^2 - y^2$	$2 x^2 - y^2$	$+\mathcal{W}_2$	$+\mathcal{V}_2$		$2t_{xz,xz}t_{yz,yz}$
1 y	1 y	$+\mathcal{W}_3$	$+\mathcal{V}_3$		$(t_{xz,xz}+t_{yz,yz})t_{xy,xy}$
2 yz	2 yz	$+\mathcal{W}_3$	$+\mathcal{V}_3$		$(t_{xz,xz}+t_{yz,yz})t_{xy,xy}$
2 xy	2 xy	$+\mathcal{W}_3$	$+\mathcal{V}_3$		$2t_{xz,xz}t_{yz,yz}$
1 y	2 yz	$+W_3$	$+\mathcal{V}_3$		$(t_{xz,xz}-t_{yz,yz})t_{xy,xy}$
$\mathcal{W}_0 = f_{-3} + \frac{5}{9} f_{-1} + \frac{1}{9} f_2 = \frac{w_1 + 4w_2}{3},$				$V_0 = \frac{8}{9}f_{-3} + \frac{10}{9}f_0 + \frac{2}{3}f_2 = \frac{4(v_1 + v_2)}{3}$	
$W_1 = \frac{3}{8}f_{-3} + \frac{11}{24}f_{-1} + \frac{1}{6}f_2 = \frac{w_1 + w_2}{2},$				$V_1 = -\frac{1}{3}f_{-3} + \frac{1}{3}f_0 + \frac{1}{2}f_2 = \frac{2v_1 - v_2}{2}$	
$W_2 = \frac{3}{4}f_{-3} - \frac{1}{12}f_{-1} - \frac{1}{6}f_2 = \frac{2w_2 - w_1}{2},$				$V_2 = \frac{2}{3}f_{-3} + \frac{1}{12}f_0 - \frac{1}{4}f_2 = \frac{2v_2 - v_1}{2}$	
$W_3 = \frac{3}{4}f_{-3} - \frac{5}{12}f_{-1} + \frac{1}{6}f_2 = \frac{w_0 + w_3}{2},$				$V_3 = \frac{2}{3}f_{-3} - \frac{5}{12}f_0 + \frac{1}{4}f_2 = \frac{v_0 + v_3}{2}$	
$\widetilde{\mathcal{W}}_0 = \frac{1}{3}f_{-3} - \frac{5}{9}f_{-1} - \frac{1}{9}f_2,$				$\tilde{V}_0 = \frac{4}{9}f_{-3}$	$-\frac{10}{9}f_0 - \frac{2}{3}f_2$
$\tilde{\mathcal{W}}_1 = \frac{1}{8}f_{-3} - \frac{11}{24}f_{-1} - \frac{1}{6}f_2,$				$\tilde{\mathcal{V}}_1 = -\frac{1}{6}f_{-3} - \frac{1}{3}f_0 - \frac{1}{2}f_2$	
$\tilde{\mathcal{W}}_2 = \frac{1}{4}f_{-3} + \frac{1}{12}f_{-1} + \frac{1}{6}f_2,$				$\tilde{\mathcal{V}}_2 = \frac{1}{3}f_{-3} - \frac{1}{12}f_0 + \frac{1}{4}f_2$	
$\tilde{\mathcal{W}}_3 = \frac{1}{4}f_{-3} + \frac{5}{12}f_{-1} - \frac{1}{6}f_2,$				$\tilde{V}_3 = \frac{1}{3}f_{-3} + \frac{5}{12}f_0 - \frac{1}{4}f_2$	



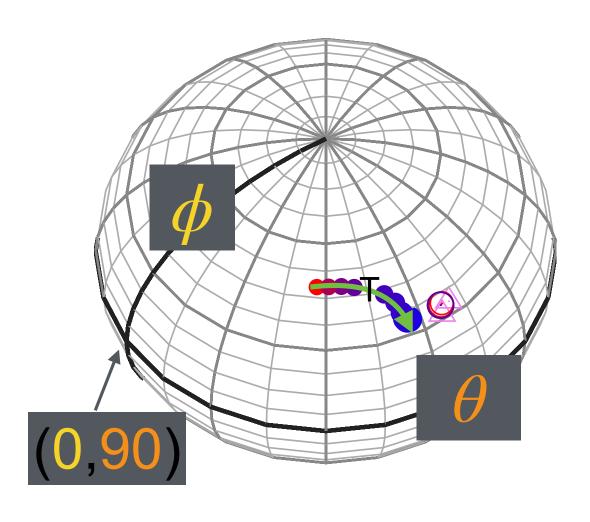
analytic & numerical



representation of orbital

$$|\theta, \phi\rangle = -|\pi - \theta, \phi \pm \pi\rangle$$

$$= \sin \theta \cos \phi |xz\rangle + \cos \theta |xy\rangle + \sin \theta \sin \phi |yz\rangle$$





empty: with CF
no T depends
if CF dominates

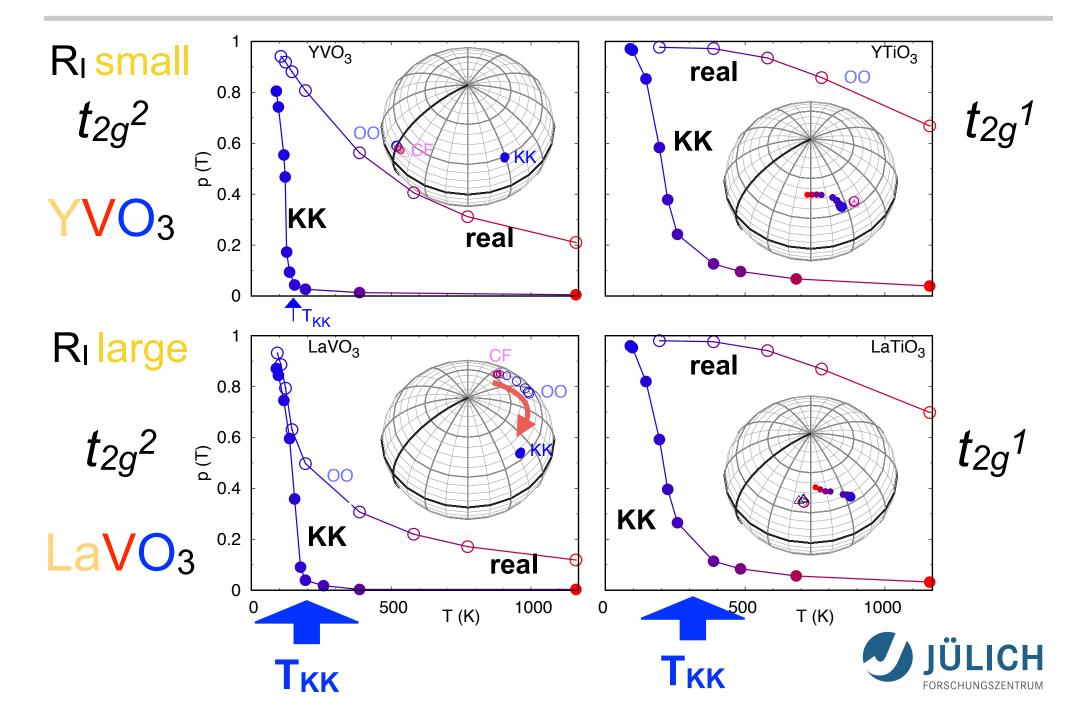


full: only KK SE

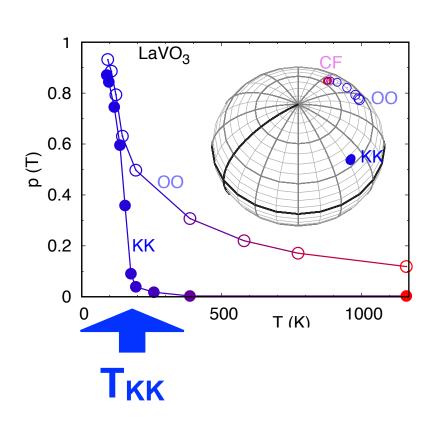
orbital rapidly changes at T_{KK}

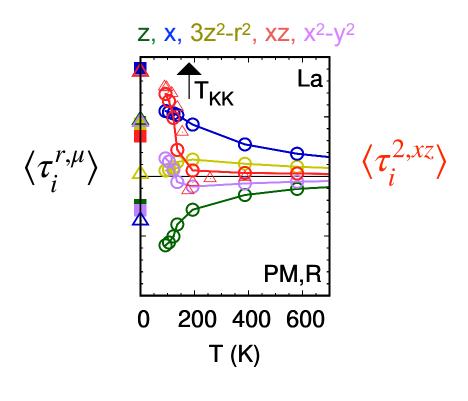


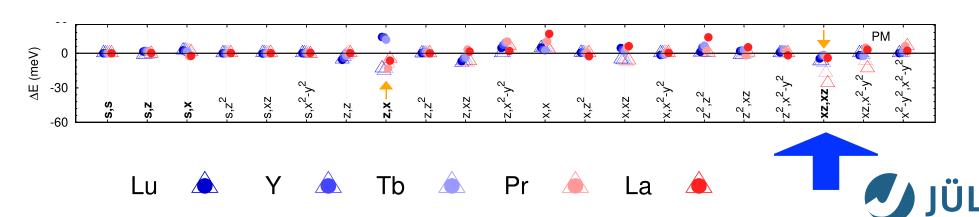
t₂g²: T_{KK}~200 K but also smaller CF



orbital channels decomposition







RVO_{3} , t_{2g}^{2} : a unique series

PRL **99,** 156401 (2007)

PHYSICAL REVIEW LETTERS

week ending 12 OCTOBER 2007

Superexchange Interaction in Orbitally Fluctuating RVO₃

J.-S. Zhou and J. B. Goodenough

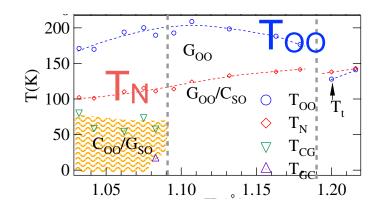
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 $LaVO_3$

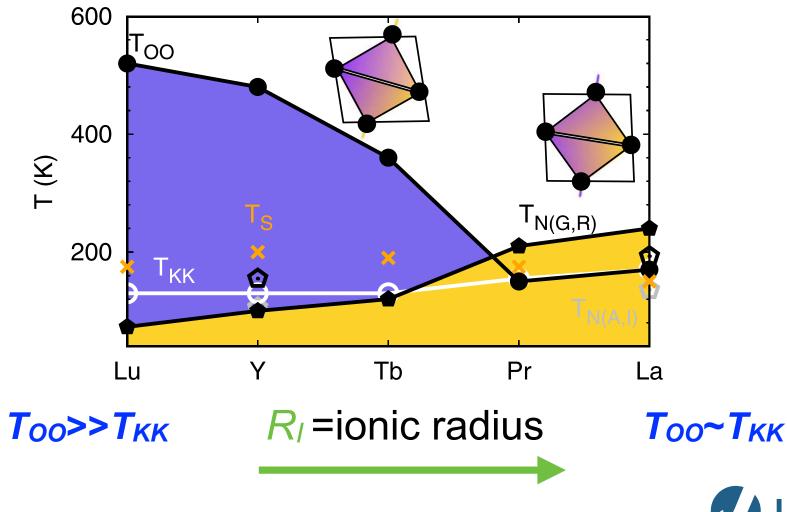
 R_{l} =ionic radius





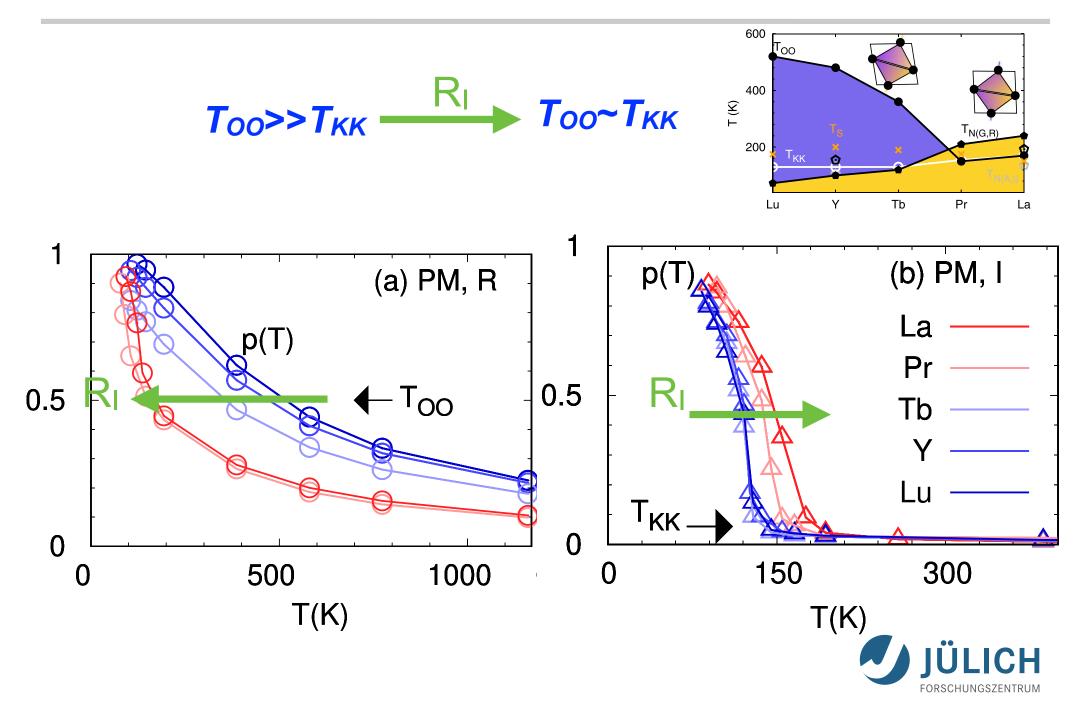
can we explain the inversion?

yes! theoretical phase diagram:



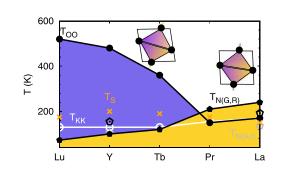


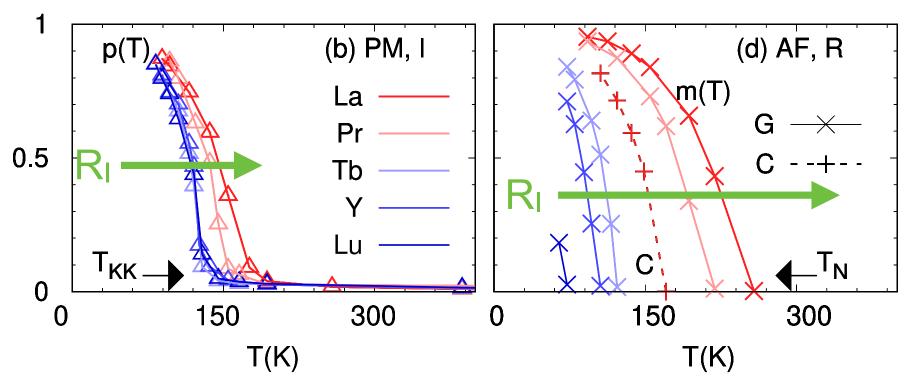
Too: evolution with R_I



T_{KK} and T_N: evolution with R_I









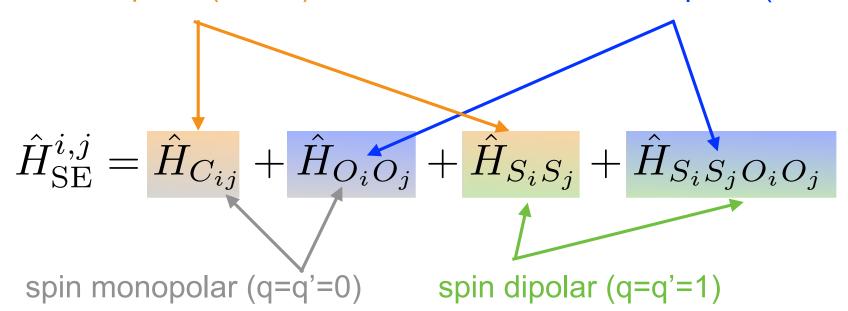


wonderful, but, why?

$$\hat{H}_{\mathrm{SE}}^{i,j} = \sum_{qq'} \sum_{\nu\nu'} \sum_{rr'} \sum_{\mu\mu'} \hat{\tau}_i^{r\mu;q\nu} D_{r\mu,r'\mu'}^{ij;q\nu} \hat{\tau}_j^{r'\mu';q\nu}$$
 r: orbital rank q:spin rank

orbital monopolar (r=r'=0)

orbital multipolar (r+r'>1)



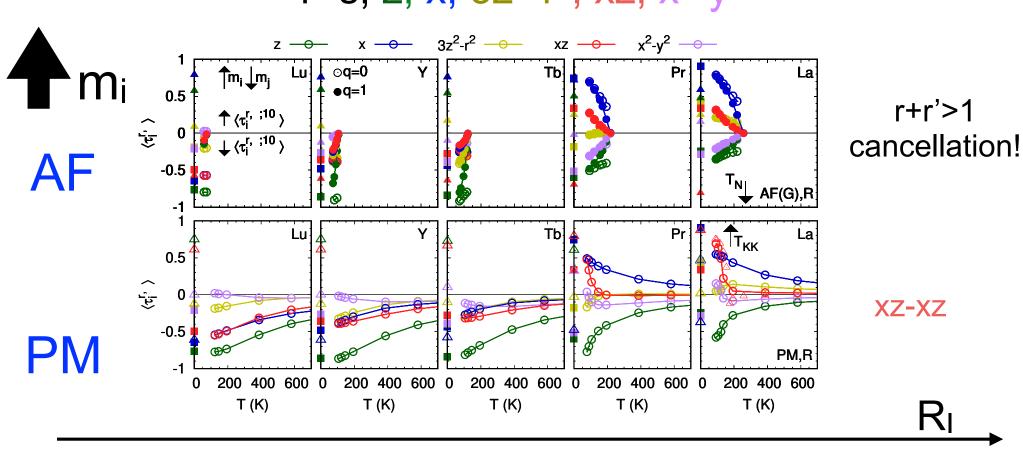
S_iS_j term main contribution to T_N!

S_iS_jO_iO_j term does the rest



spin-orbit S_iS_iO_iO_i channels

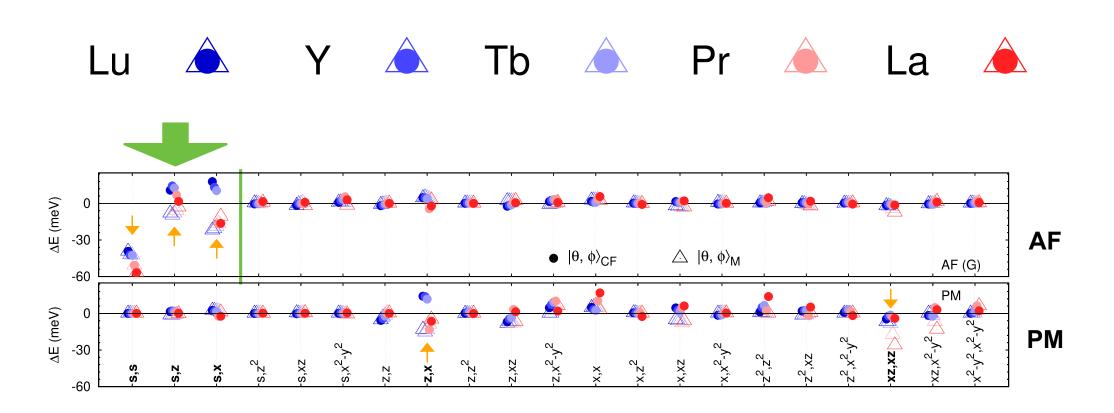
$$r=s, z, x, 3z^2-r^2, xz, x^2-y^2$$



strong spin-orbital entanglement



idealized magnetic state



AF: orbital "Zeeman" term dominate



conclusions

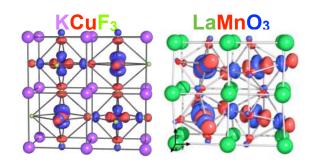
(i) are there true Kugel-Khomskii materials?

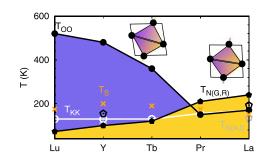


Yes! t_{2g} systems better than e_g signatures are electronic

(ii) why (usually) Too>T_N ?

in most systems T₀₀>>T_{KK}





but if T_{KK}-T_{OO}, T_N and T_{KK}-T_{OO} can be flipped G-type magnetic ordering is better



